



# Turbulenter Impuls- und Wärmetransport in Flüssigmetallen- Experimentelle Methoden und Berechnungsansätze

**Stieglitz, R.**

Batta, A., Grötzbach, G., Class, A., Daubner, M., Lefhalm, C.-H.,  
Otic, I.  
and the KALLA team

Institute for Nuclear and Energy Technologies (IKET)  
Forschungszentrum Karlsruhe GmbH



# Content

- Technical appearance of liquid metal flows
- Specific properties of liquid metals
- Turbulent heat exchange
  - Analogies between momentum and heat exchange
  - Experimental observations in a heated pipe
  - Closure methods for turbulent heat flux
- Measurement techniques in liquid metals
- Engineering applications
  - The heated pipe an old story
  - Heated Rod in a cylindrical cavity in KALLA
  - MEGAPIE target
- SUMMARY and outlook



# Technical Liquid Metal flows

- Liquid metals are known to mankind since about 6000 years (natural Mercury)
- They are refined and casted since more than 4000 years (bronze, copper)
- Production of iron started in Turkey since 3000 years
- Alumina and alloy production on large scales in the last 200years
- Current industrial interest:
  - Adaptive materials with certain properties for specific use in e.g. car industry, aeronautics, etc. like ALi-alloys
  - Minimization of primary energy input during refinement
  - Higher demand on quality of surfaces and reduction of number of secondary machining processes



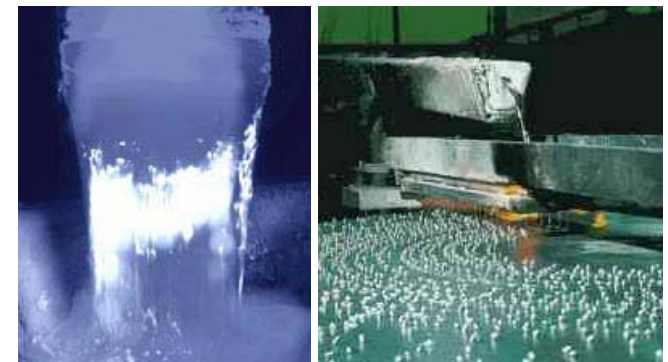
Liquid mercury in glass capsule



Bronze casting



Raw iron refinement



Alumina preparation for casting

➔ Requirements:  
Measurement techniques, heat transport phenomena,  
phase change problems



# FISSION: MYRRAH

- a planned 50MW Experimental ADS

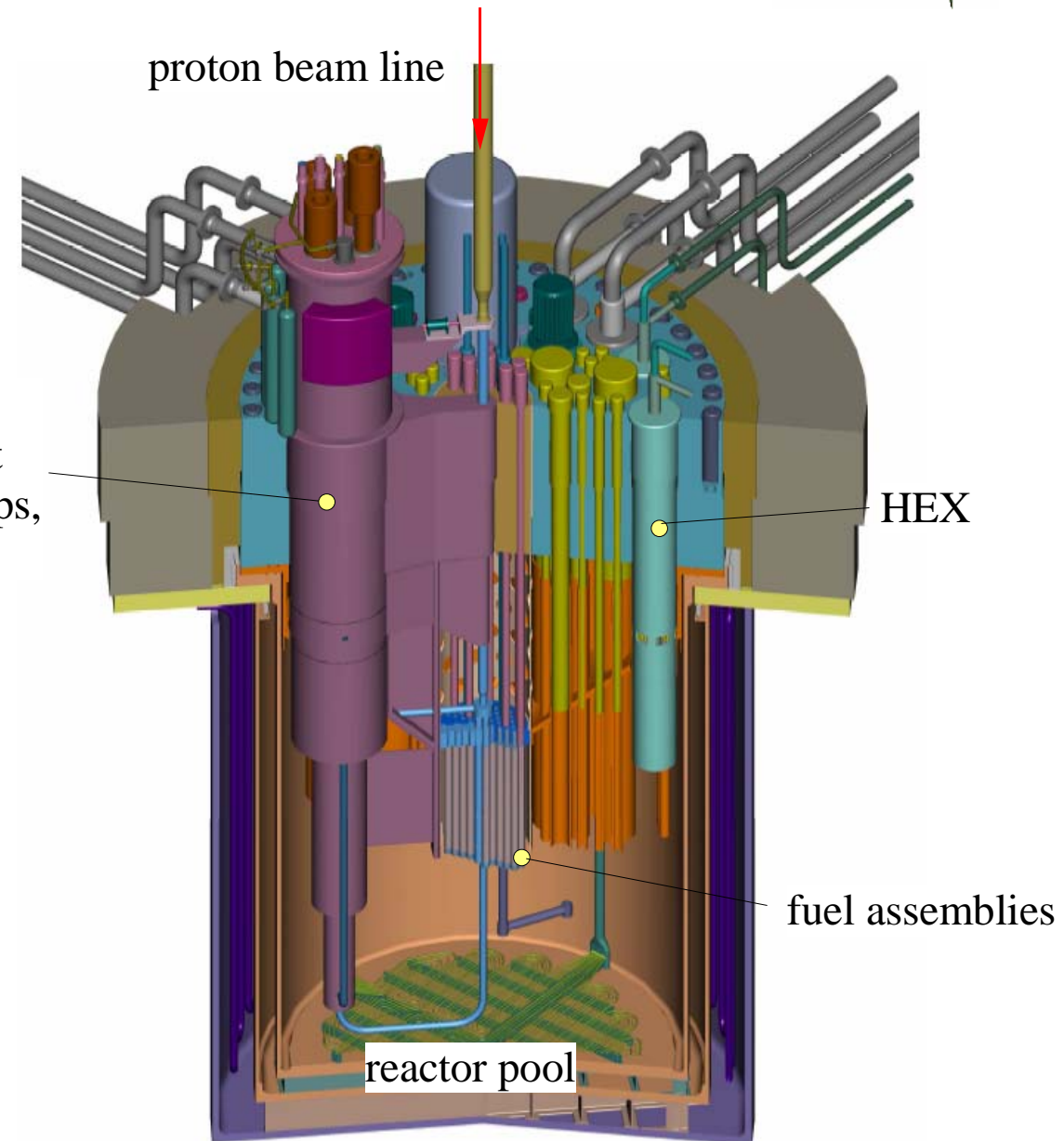
## Features

- Free surface target
- Criticality  $k_{\text{eff}} \sim 0.95$
- Thermal power  $P_{\text{th}} = 50\text{MW}$
- Proton beam 350MeV at 5mA
- Lead bismuth cooled

## Critical thermal hydraulic issues

- Free surface flows with turbulence
- Mixed convection (Buoyancy) in the core
- LM technology in Target and Core
- Instrumentation and monitoring

removable  
Target unit  
(incl. Pumps,  
HEX, etc.)







# Specific properties of liquid metals

## GENERAL FEATURES

- opaque, totally reflecting
- high temperatures,
- corrosive,
- large surface tension
- high thermal conductivity

## HEAVY LIQUID METALS

- high density
- low kinematic viscosity,

		Unit	Pb <sup>45</sup> B <sup>i55</sup>	Lithium	Water
			300°C	300°C	25°C
density	$\rho$	[kg/m <sup>3</sup> ]	10325	505	1000
heat capacity	$c_p$	[J/(kgK)]	146.33	4279	4180
kinematic viscosity	$\nu$	[m <sup>2</sup> /s]·10 <sup>-7</sup>	1.754	9	9.1
heat conductivity	$\lambda$	[W/(m K)]	<b>12.68</b>	<b>29.2</b>	0.6
electric conductivity	$\sigma_{el}$	[A/(V m)]·10 <sup>5</sup>	<b>8.428</b>	<b>33.5</b>	2·10 <sup>-4</sup> (tap)
thermal expansion coefficient	$\alpha$	/	<b>6.7·10<sup>-3</sup></b>	<b>43.6·10<sup>-3</sup></b>	6·10 <sup>-3</sup>



# Specific properties of liquid metals

Force ratio		$X_{\text{PbBi}(300^\circ\text{C})}/X_{\text{Water}(25^\circ\text{C})}$	$X_{\text{Li}(300^\circ\text{C})}/X_{\text{Water}(25^\circ\text{C})}$	Energy ratio		$X_{\text{PbBi}(300^\circ\text{C})}/X_{\text{Water}(25^\circ\text{C})}$	$X_{\text{Li}(300^\circ\text{C})}/X_{\text{Water}(25^\circ\text{C})}$
Reynolds	$Re = \frac{u \cdot l}{\nu}$	<b>5</b>	0.98	Peclet	$Pe = \frac{u \cdot l}{\kappa}$	<b>0.017</b>	<b>0.01</b>
Grashof	$Gr = \frac{g \cdot \alpha \cdot \Delta T \cdot l^3}{\nu^2}$	<b>30</b>	<b>7.4</b>	Fourier	$Fo = \frac{l^2}{\kappa \cdot t}$	0.017	0.01
Prandtl	$Pr = \frac{\nu}{\kappa}$	<b>0.003</b>	<b>0.008</b>	heat conduct. [m <sup>2</sup> /s]	$\kappa = \frac{\lambda}{\rho \cdot c_p}$	<b>58.5</b>	<b>94.1</b>

- Scale separation of thermal and viscous boundary layer



## Strategy (EU, HGF and internal programs)

- Liquid metal adapted heat transfer models (several approaches possible)
- Detailed measurements in simple geometries (model development and verification, statistical features of u and T, measurement technology)



# Turbulent heat transfer

- Turbulent energy equation

$$\rho c_p \left( \bar{u} \frac{\partial \bar{T}}{\partial x} + \bar{v} \frac{\partial \bar{T}}{\partial y} \right) = - \frac{\partial}{\partial y} \left( - \lambda \frac{\partial \bar{T}}{\partial y} + \rho c_p \overline{v' T'} \right) ,$$

- Analogous to the turbulent viscosity  $\varepsilon_M = \mu_t / \rho$  a turbulent heat flux appears and thus
- a turbulent eddy heat diffusivity  $\varepsilon_H = \lambda_t / (\rho c_p)$  can be defined, the ratio is called
- the turbulent Prandtl number  $Pr_t$

$$Pr_t = \frac{\varepsilon_M}{\varepsilon_H} = f \left( Re, Pr, \frac{y}{R} \right) = \frac{\overline{u' v'}}{\overline{v' T'}} \frac{\frac{\partial T}{\partial y}}{\frac{\partial u}{\partial y}}$$

## Consequences

- $Pr_t$  is far of being a constant (in reality a tensor)
- Difficult to measure directly (measure of dimensions and available sensor sizes, temporal resolution)
- Involves several modelling problems



# Turbulent heat transfer

## Closure methods for turbulent heat flux

- Semi-empirical models of zero and first order developed since late fourties yield mostly to **Reynolds analogy** results and to  $Pr_t = f(Pr, \varepsilon_M / \nu)$  (momentum-field  $\approx$  temperature field)
- Turbulent Prandtl  $Pr_t$  number from analytic solutions account for the statistics of the turbulence field (see Yakhot et al., 1987), but only applicable to simple geometries problematic with buoyant flows.

$$\left[ \frac{(Pr^{-1} - 1.1793)}{(Pr^{-1} - 1.1793)} \right]^{0.65} \left[ \frac{(Pr^{-1} + 2.1793)}{(Pr^{-1} + 2.1793)} \right]^{0.35} = \frac{1}{(1 + \varepsilon_M / \nu)} \quad \text{with} \quad Pr_{eff} = \frac{(1 + \varepsilon_M / \nu)}{\left( \frac{\varepsilon_M / \nu}{Pr_t} + \frac{1}{Pr} \right)} .$$

- Turbulent heat transport modelling by means of transport equations ( e.g. the turbulent fluxes  $\overline{u_i' T'}$  temperature variance  $\overline{T'^2}$ , and its dissipation  $\varepsilon_T$  (TMBF –model) but each higher level of modelling leads to new constant and triple correlations a priori not known.  
Potential Solution approach:  
Determination of constants and triple correlations from
- Direct numerical simulation of the temperature field in simple geometries
- CURRENT STATUS: sophisticated models for  $u$ -field but 0-dim. for  $T$ -field





# Velocity: Intrusive methods

## ■ Pitot and Prandtl tubes

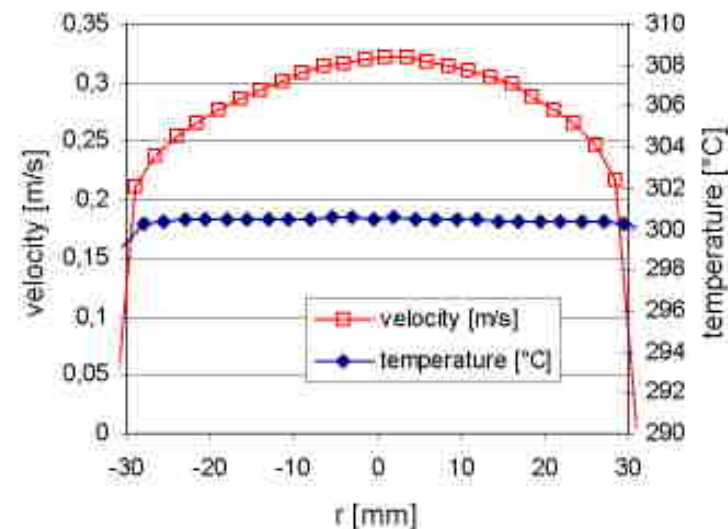
measurement of pressure or pressure differences in fluid domains (coupled with TC)

### Advantages

- Sufficient time resolution
- Simple set-up

### Disadvantages

- Disturbance of flow (intrusive method)
- Limited spatial resolution (boundary layer)
- Several corrections required.
- High fabrication effort in miniaturizing
- Sophisticated fill and drain necessary.
- Variable measurement ranges necessary for resolution of smallest fluctuations.
- Only one component measurable (flows in complex geometries ?)





# Velocity : Ultra-Sound Doppler Velocimeter (UDV)

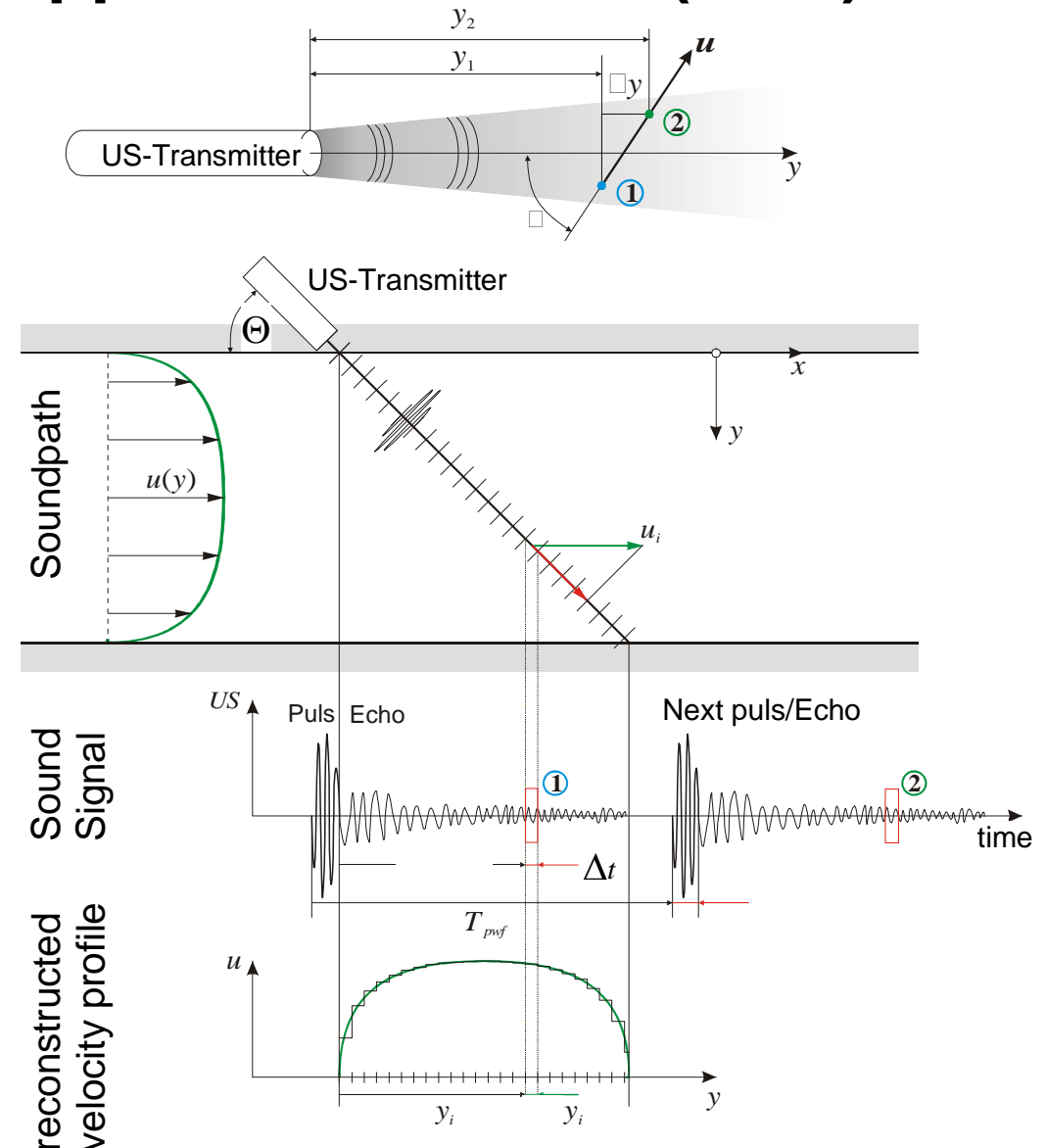
## Principle (particle tracking)

- Distance change from sensor due to motion from 1 → 2 between two pulses.
- Determination of the time difference from the phase shift between received echoes

➔ Velocity at a discrete distance

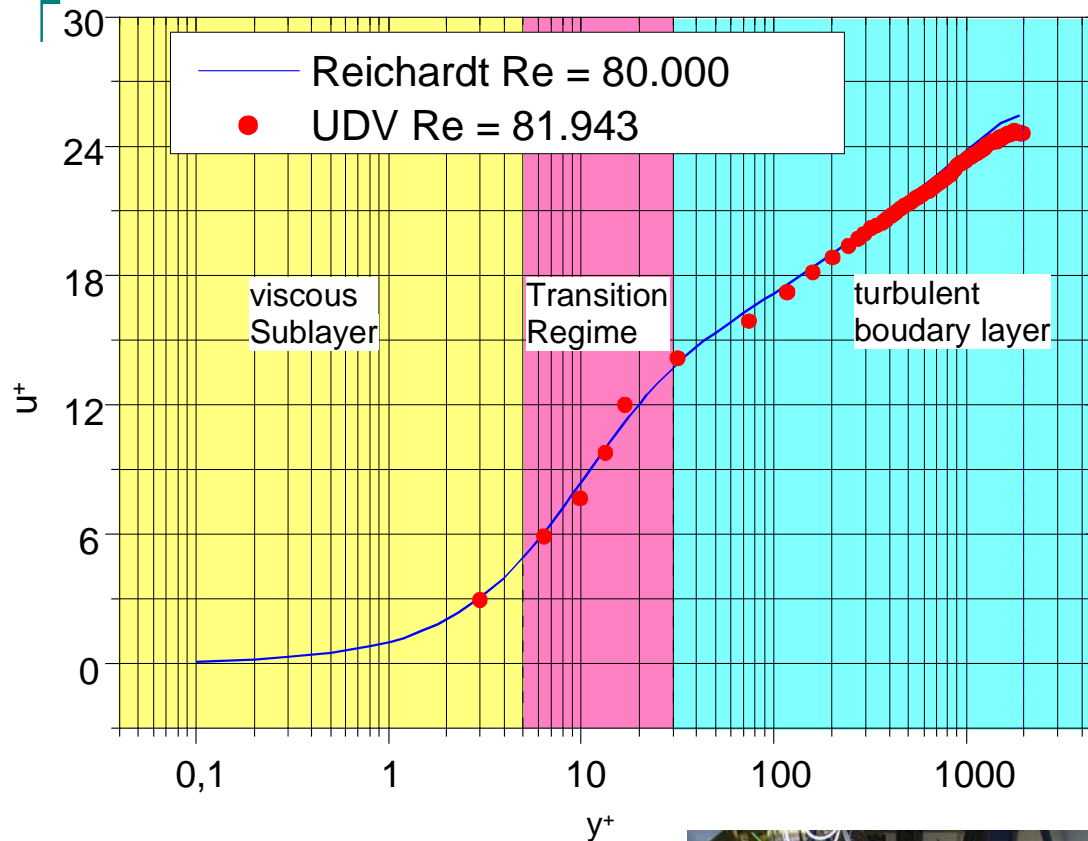
## Profile

- Separation of sound path in time intervals (gates  $\Delta t$ ) allows recording of a velocity profile. Therefore,
  - Coupling of a time  $t_i$  with a measurement position
  - Determination of the local velocity  $u_i$  in the interval  $i$

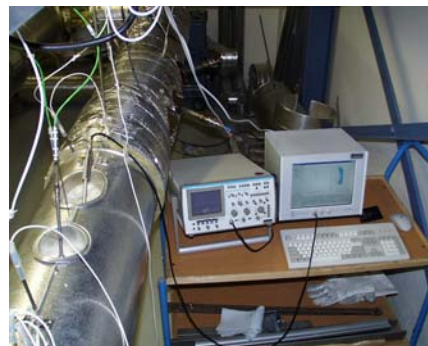




# Velocity: Ultra-Sound Doppler Velocimeter (UDV)



UDV-Sensor developed  
in cooperation with  
FZR



## Result in the boundary layer

- All parts of the viscous boundary captured by UDV
- Max. deviation in the transition regime of 5%
- UDV-measurements possible into the viscous sublayer ( $y^+ = 3 \sim 46 \mu m$ )
- Temporal resolution currently up to 30Hz

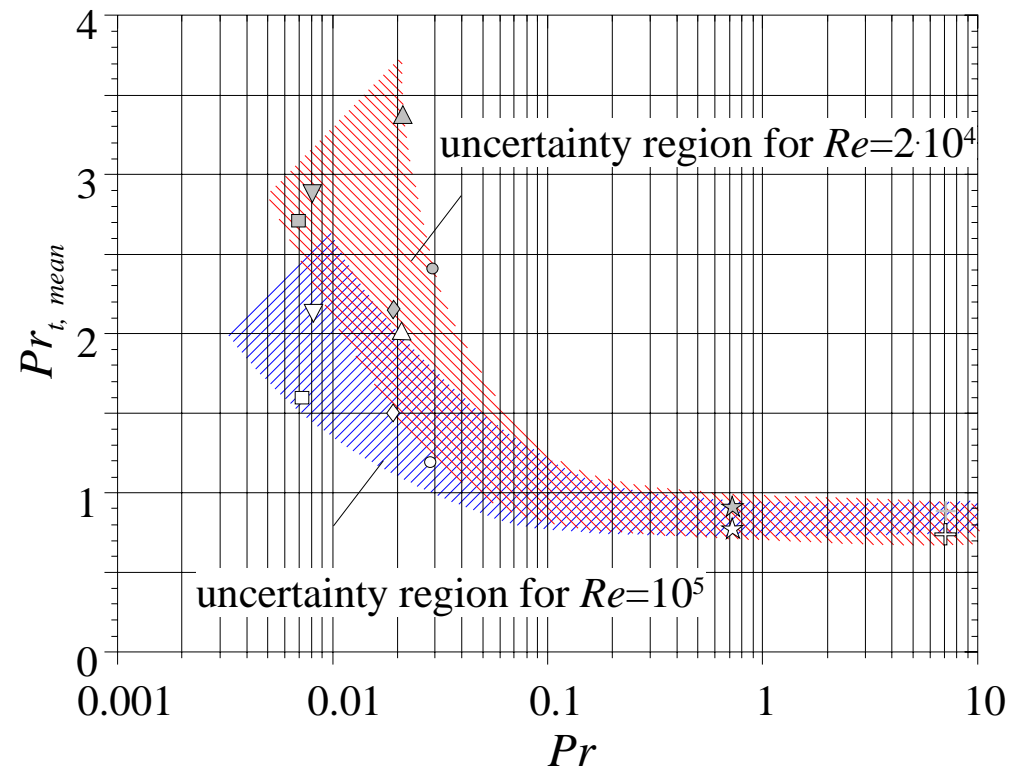
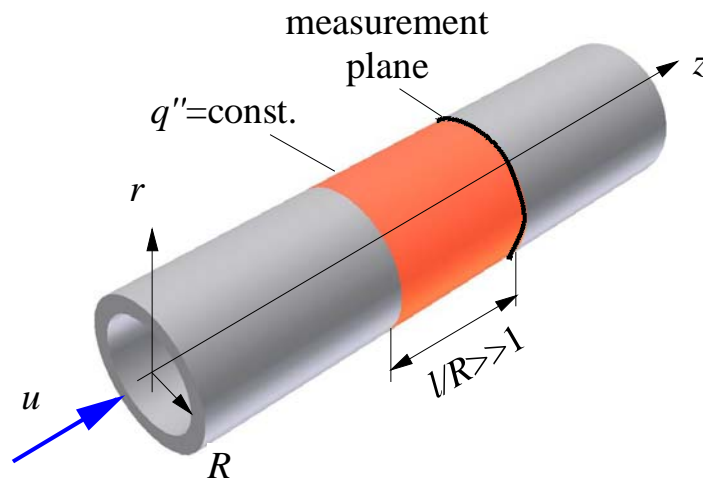
## Problems

- Long-term wetting of the sensor
- Temporal resolution (Turbulence spectra)
- What are the scattering particles ?
- More effective wave guides (Temperature, sound losses)
- Enhancement of math algorithm effectivity
- Only applicable in isothermal flows.
- Only one velocity component (3D-flows ?)



# The Heated Pipe- “An old Story”

Fully developed turbulent (hydraulically and thermally) flow heated with a constant heat flux at different Reynolds ( $Re$ ) and molecular Prandtl numbers ( $Pr$ )



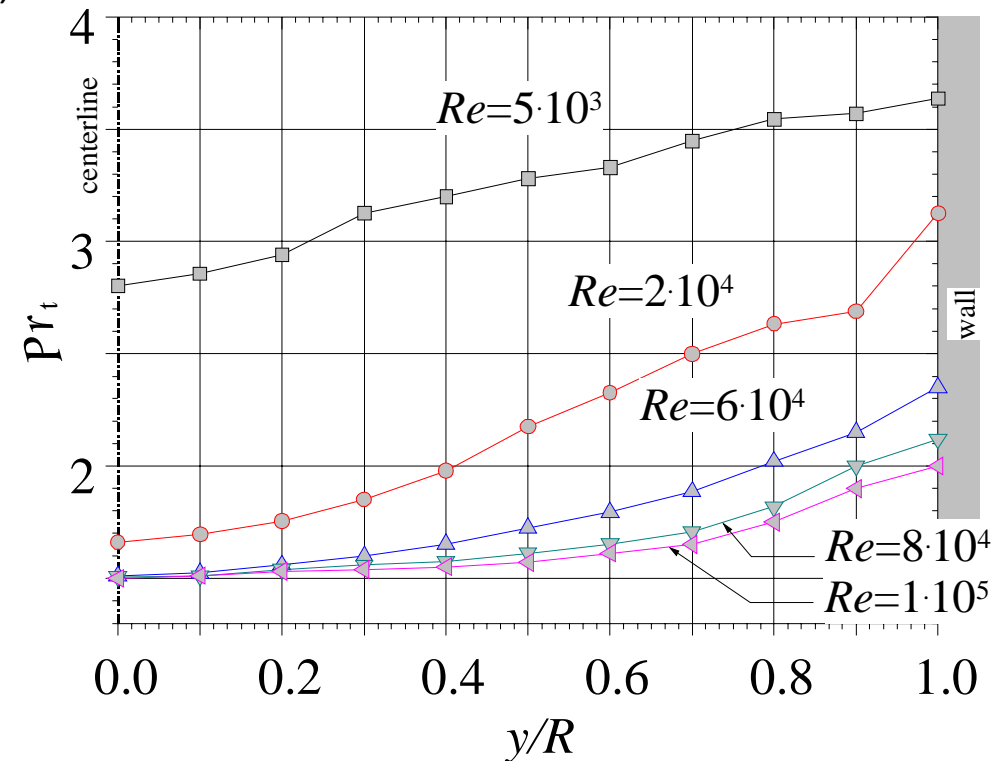
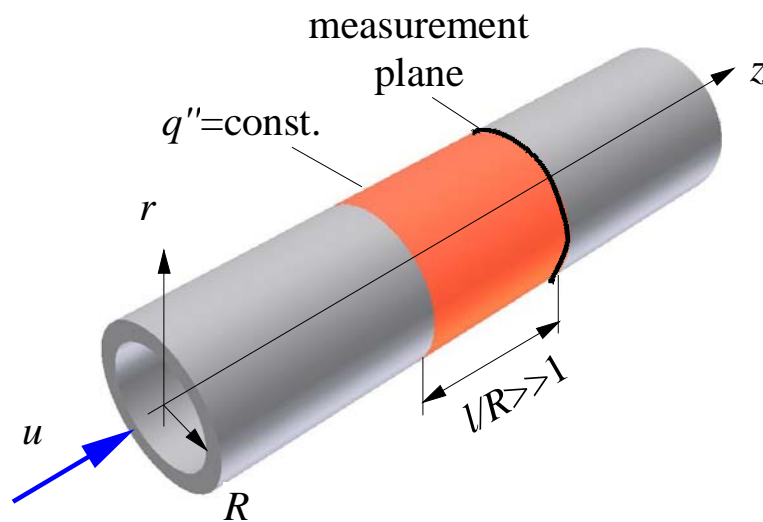
## ■ Result:

- Mean turbulent Prandtl number ( $Pr_{t,mean}$ ) depends on molecular Prandtl number  $Pr$ .
- Mean turbulent Prandtl number ( $Pr_{t,mean}$ ) is a function of the Reynolds number  $Re$ .
- But, for model development an unacceptably large uncertainty exists.



# The Heated Pipe- “An old Story”

- Measured local turbulent Prandtl number ( $Pr_t$ ) in a fully developed turbulent flow heated with a constant heat flux at different Reynolds ( $Re$ )



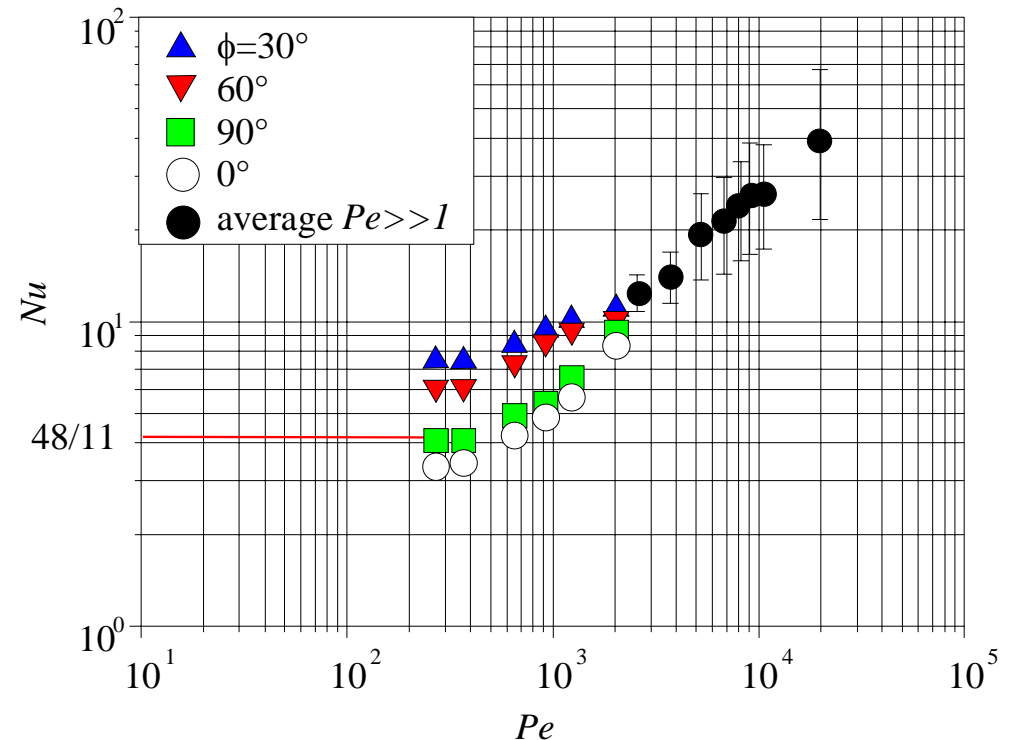
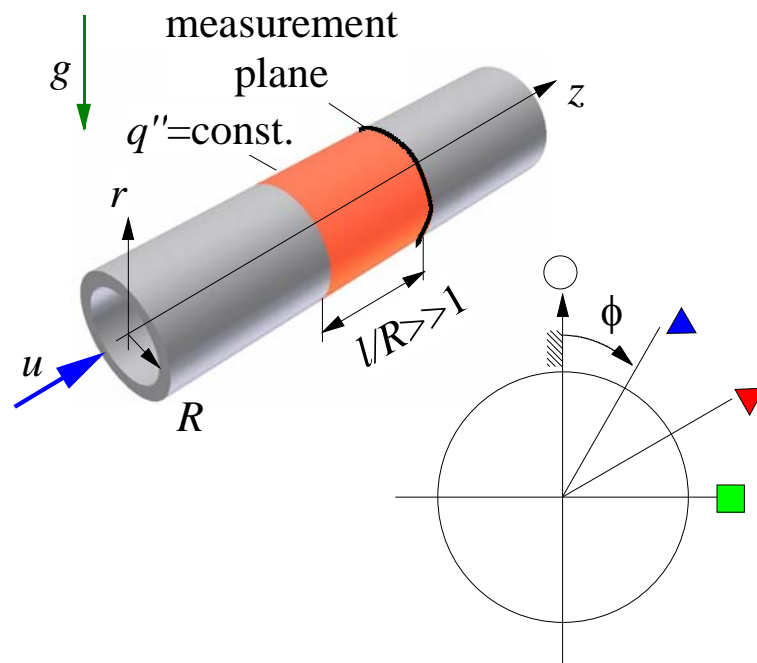
- Result:
  - Local turbulent Prandtl number ( $Pr_t$ ) is a function of the Reynolds number  $Re$  and the radial coordinate  $y/R$ .
  - But, be careful with experimental data because boundary conditions and buoyancy play a considerable role.





# The Heated Pipe- “An old Story”

- The problem of free convection distortion. Liquid metals exhibit due to their large thermal expansion and low kinematic viscosity buoyancy distortion effects even at large  $Re$  (Hg, PbBi at  $Re > 10^5$ )
- The horizontal pipe

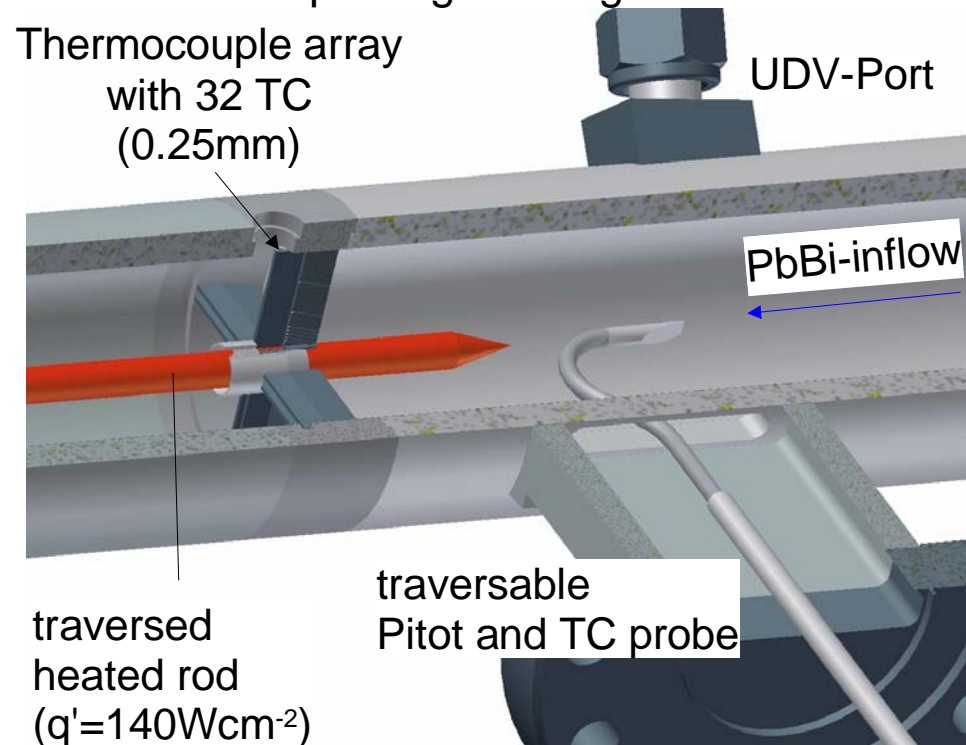


- Result:
  - Even large  $Re$  does not ensure a pure forced convective flow.



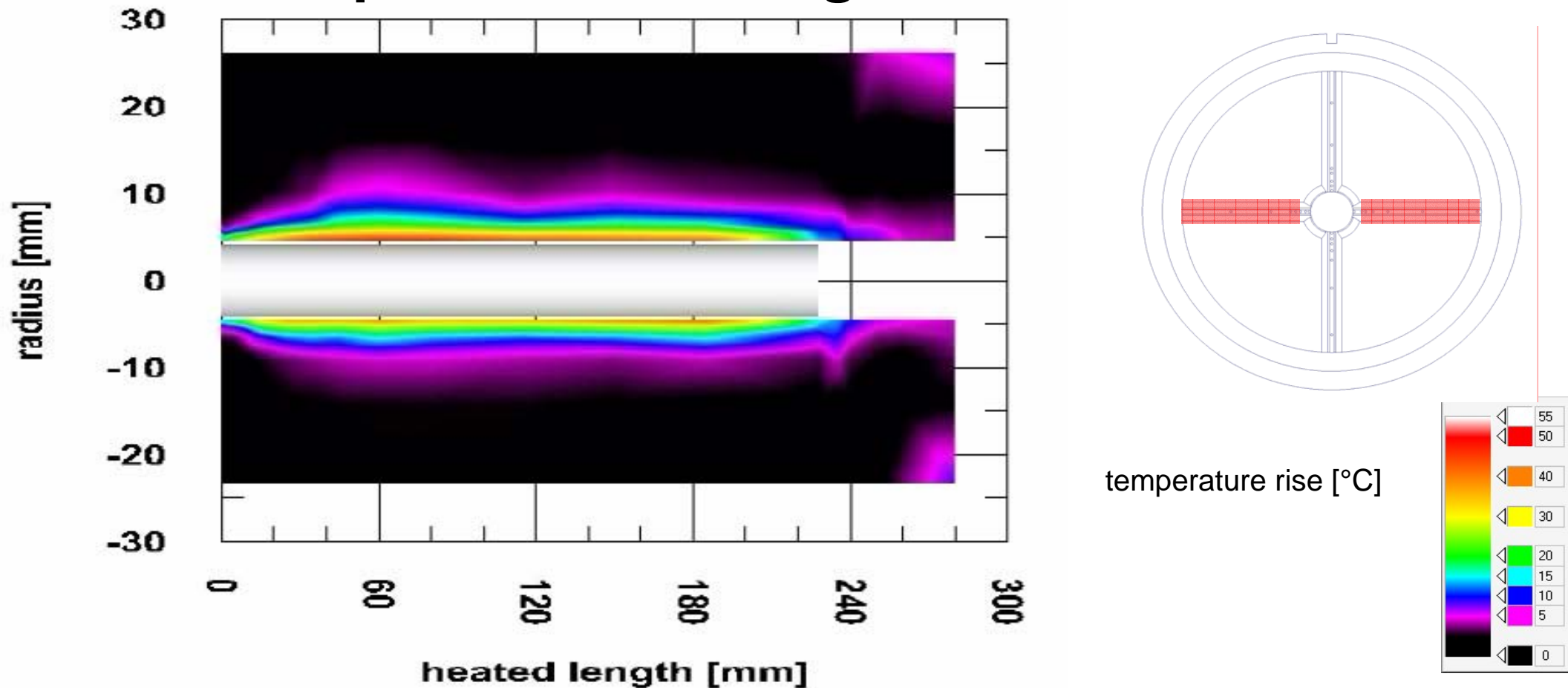
# The Heated Rod in THESYS(KALLA)

- Fully developed turbulent flow facing a heated rod concentrically in an annular cavity.
- Horizontal arrangement with defined boundary conditions regarding
  - Detailed measurement of the inflow velocity profile
  - Local velocity and temperature measurements.
  - Heat balance and heat loss evaluation (monitoring temperatures at outside insulation).
  - Pre- and post test analysis of the test section.
- CFD analysis with commercial code packages using different turbulence models.





# Temperaturfeld along the Heated Rod



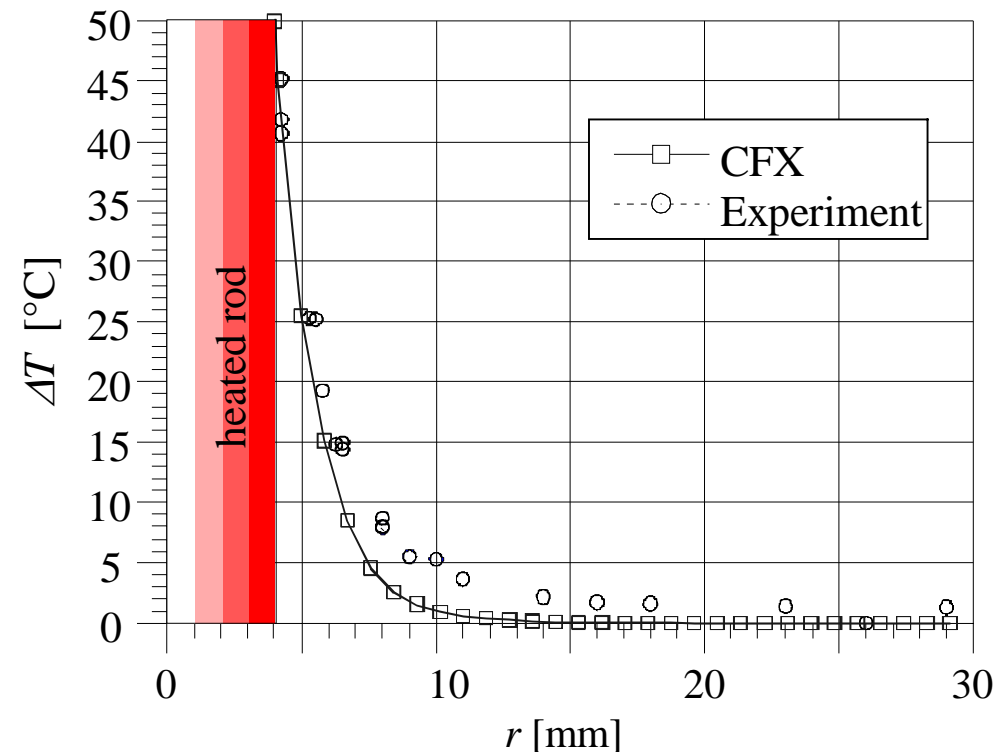
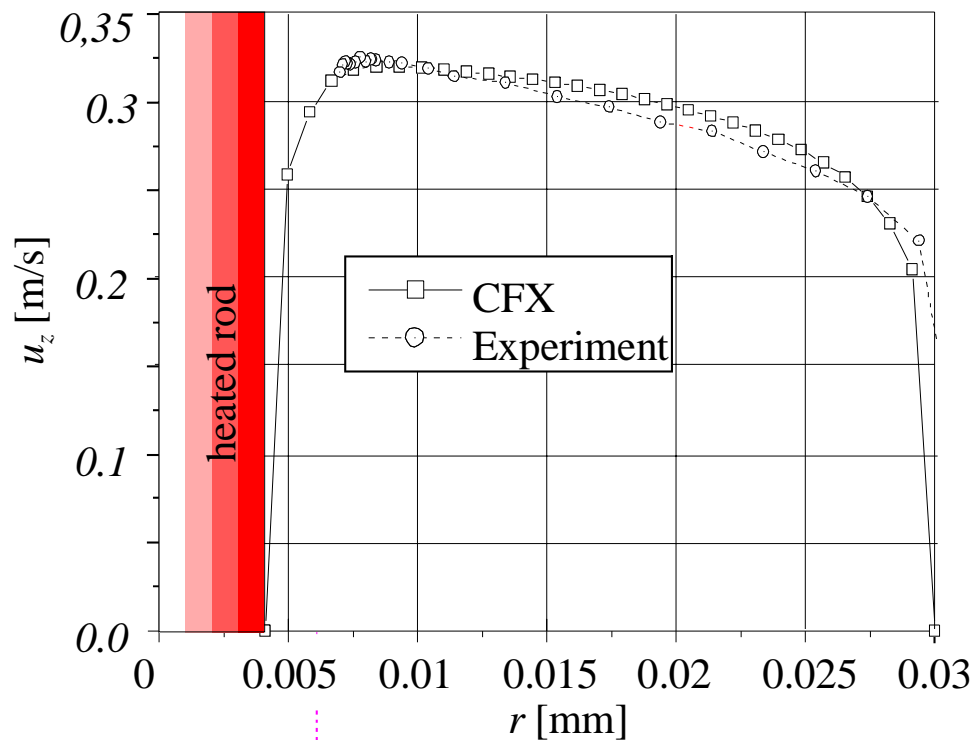
Conditions:  $Re = 10^5$ ,  $P_{HR} = 2\text{kW}$ ,  $T_{in} = 300^\circ\text{C}$

- Only in front part a symmetric temperature profile
- Distortion of the temperature field for  $z/d > 13.9$  (asymmetry of rod, buoyancy)



# The Heated Rod-CFD

- CFD with SST-model ( $k$ - $\Omega$ -model near wall and  $k$ - $\varepsilon$  in the bulk),  $y^+ \sim 1$  in heated part, but use of Reynolds-analogy between  $u$  and  $T$  field with a prescribed and constant  $Pr_t$  (mostly  $Pr_t = 0.9$ ),



Conditions:  $Re = 10^5$ ,  $P_{HR} = 2\text{kW}$ ,  $T_{in} = 300^\circ\text{C}$  at  $z/d = 13$  (half heated length)

- Coincidence of measured and computed velocity.
- Reasonable temperature agreement of CFD with Experiment at fluid- wall interface. But,
- Thermal boundary layer is thicker in experiment like expected (different heat fluxes).



# MEGAPIE – Liquid metal cooled “Beam window”

## Features

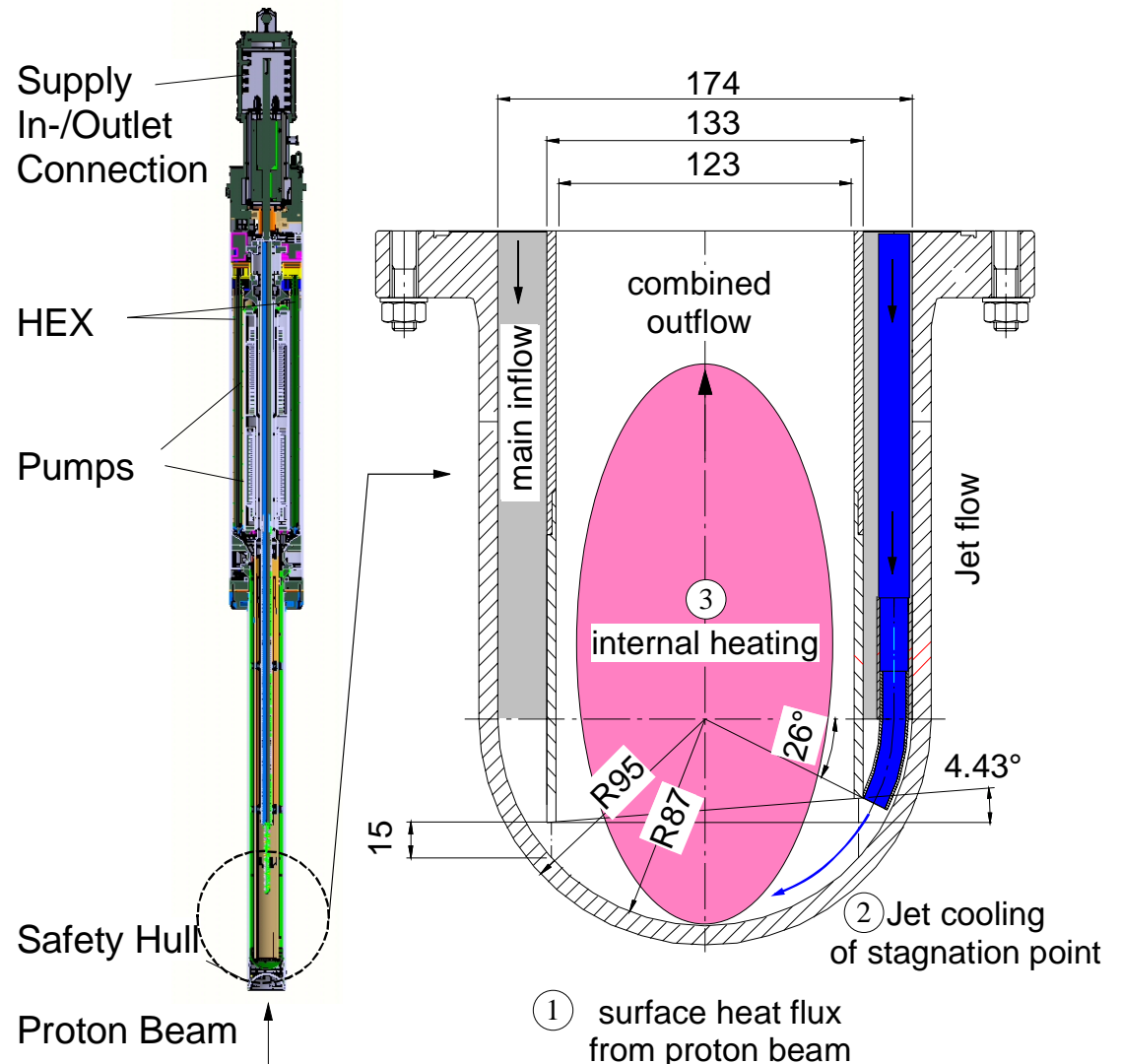
- 1MW power release in spallation target
- 82 litres PbBi-inventory containing pump, HEX, cover system, etc.

## THERMALHYDRAULICS

- Complex flow in 3D geometry
- Internal heat generation by spallation reactions (85-92%).
- Surface heat removal from proton heated “beam window” (8-15%).
- Jet cooling of stagnation point (turbulent mixing of heat by cross flow).

## AIM

- Spallation demonstration
- Neutron source for Physics
- Full power operation since Aug. 2006





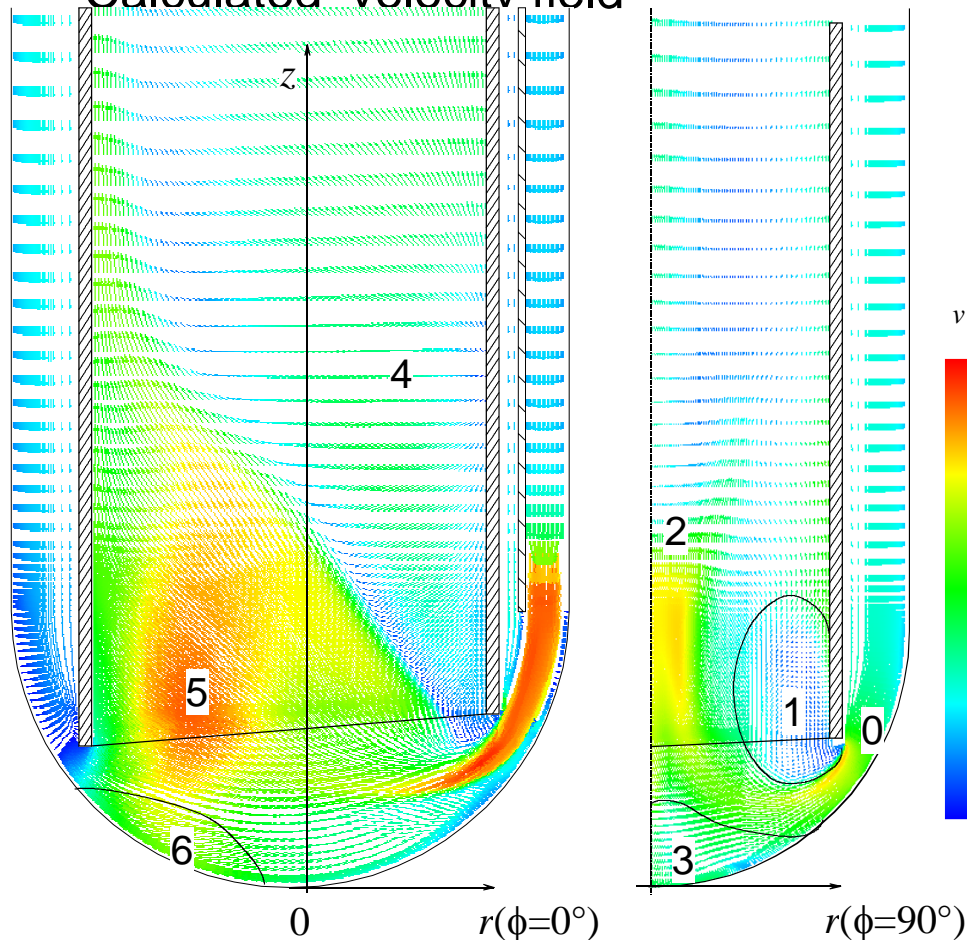


# MEGAPIE-Simulation-Heated Jet Experiment

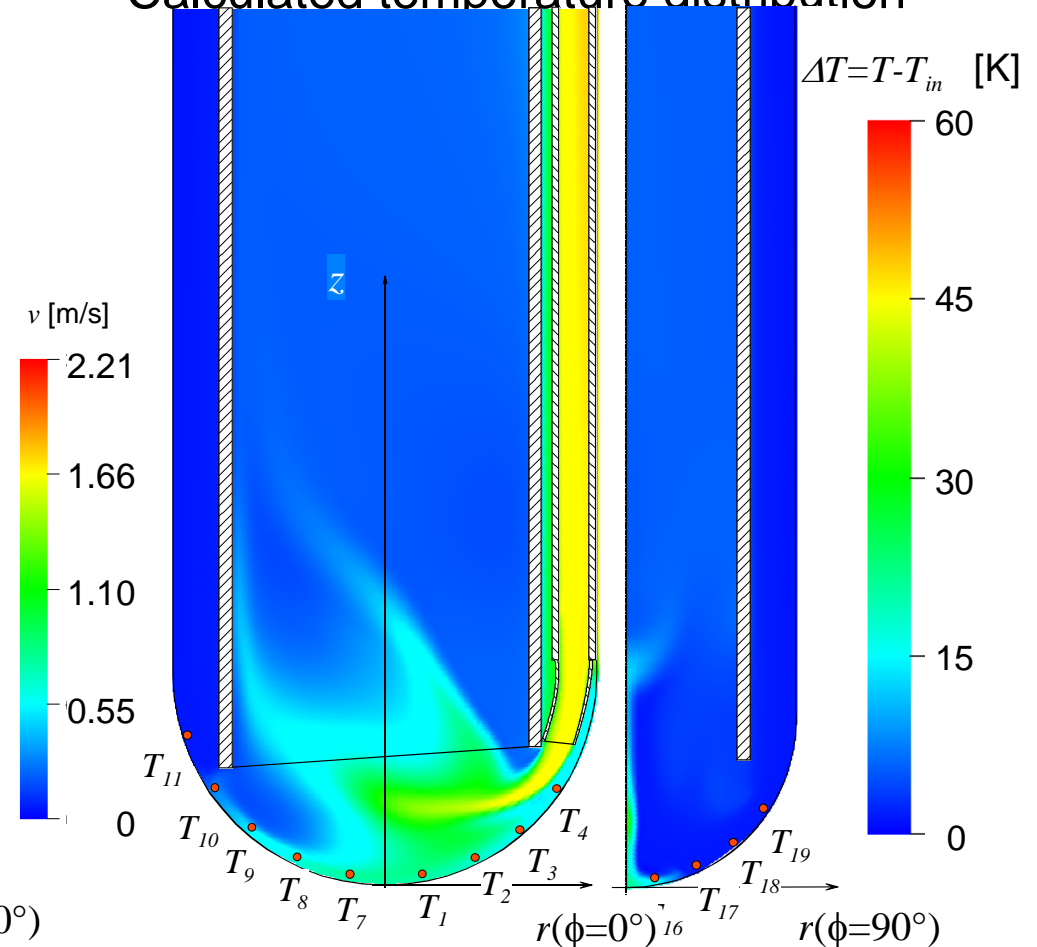
CFD (SST, Reynolds –analogy, symmetry assumption) simulation of the

- momentum field in a complex geometry and the corresponding
- temperature field.

Calculated velocity field



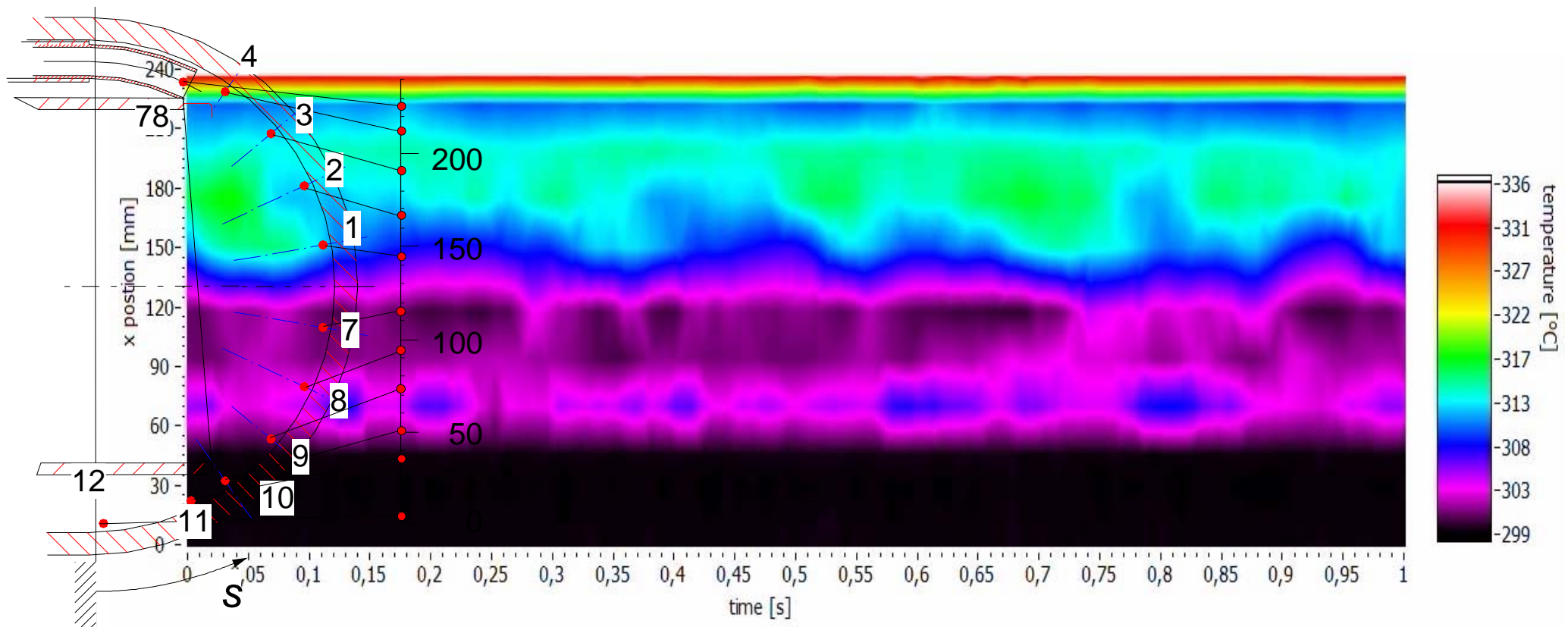
Calculated temperature distribution





# MEGAPIE -Heated Jet Experiment

Temporal behavior of the temperature distribution at the lower shell in nozzle plane  
for  $Q_{\text{main}}=18\text{m}^3/\text{h}$ ,  $Q_{\text{jet}}=1.2\text{m}^3/\text{h}$ ,  $T_{\text{in}}=300^\circ\text{C}$ ,  $T_{\text{jet}}=360^\circ\text{C}$ ,  $f_{\text{recording}}=128\text{Hz}$ .



- Jet impinging the lower shell 60mm away from center line and splitting up into different streams.
- Part of jet stream hitting shell opposite the nozzle exit.
- Temperature field time dependent at nominal operation conditions strong fluctuations at centerline ((→LES))



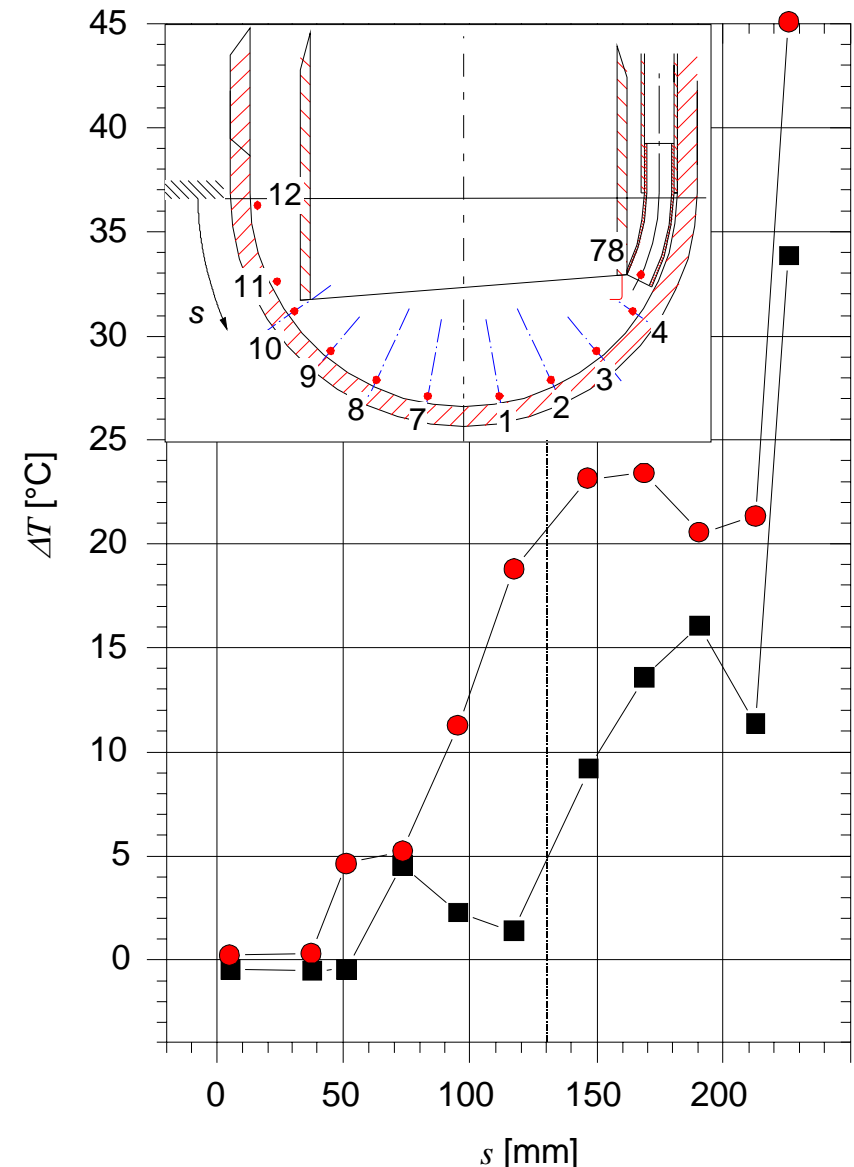
# MEGAPIE-CFD-EXPERIMENT

## *Temperature distribution in the lower shell in nozzle plane (experiment-simulation)*

- (1) Significant differences already at calc. inlet temperature.
  - Experiment different to model (history),
  - Inadequate turbulence model.
- (2) No double peaks in simulation an jet covering the center line.
  - different geometry (differential elongation and change of exp. configuration)
  - different velocity distribution (exp.-CFD) because of complex geometry (expressed by non-symmetric  $T$ -Profiles)

## Consequence

Detailed analysis of both experimental and CFD data is an **iterative process**





# SUMMARY of LIQUID METAL HEAT TRANSFER

## Turbulent heat exchange modelling

- State of the art  $Pr_t$ -correlations in codes!,
- Better buoyant flow modeling (+Qualified user),
- At least ASM based turbulent heat flux models ( $u'T'$ )
- DNS required to improve and validate advanced heat flux models to be embedded in commercial codes

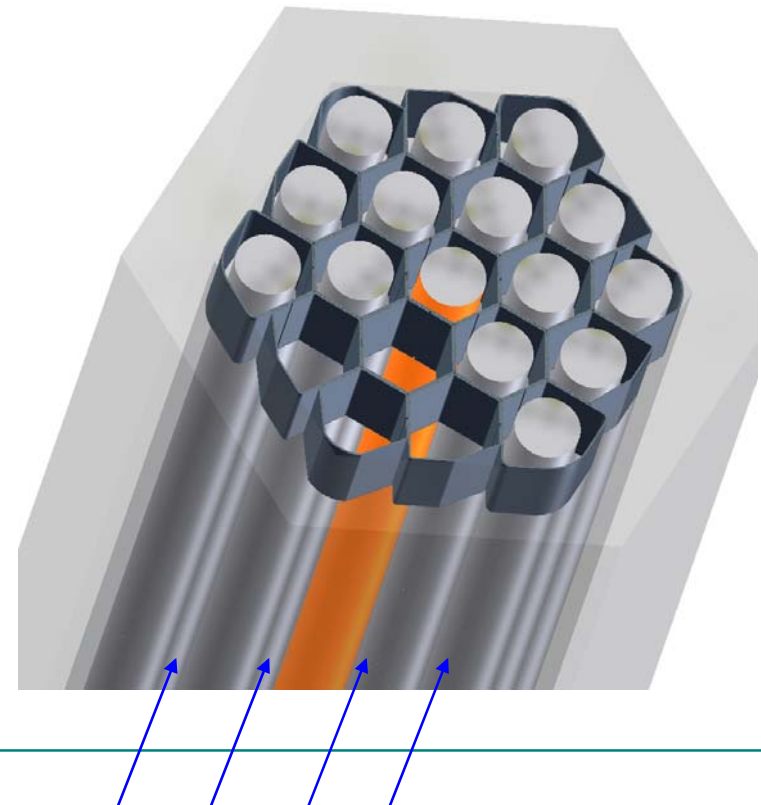
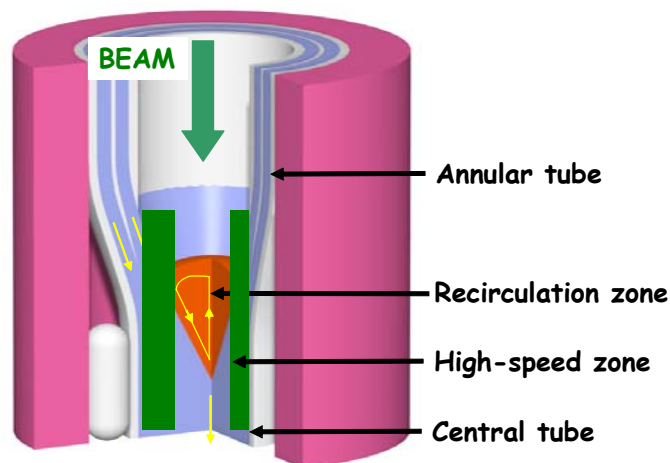
## MEASUREMENT TECHNIQUES

- Improved sensors to capture local flow velocities (accuracy, multi-components and spatial and especially temporal resolution, best non-intrusive)
- Defined benchmarks (regarding CFD, LES and DNS but also related to the BC's with supplementary water experiments)



# OUTLOOK at KALLA

- Repetition of heated rod with  $u'$ ,  $v'$ ,  $u'T'$ ,  $T'^2$  and related mean values
  - Accompanying CFD and potentially DNS (ressources)
- Experiments in rod bundles
  - Water experiments with optic means (LDA,LLS,PIV)
  - Liquid metal teat transfer in bundle flows (Local  $T$ ,  $T'$ )(mixed, forced and buoyant)
- Free surface target
  - Surface position (stability, meas. technique)
  - CFD modelling (Level-Set, com. codes)







# SUPPLEMENTARY FIGURES



# CFD-Calculation strategies for liquid metal flows

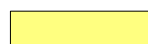
Model-Procedure	Momentum	Heat	Time horizon	Comment
Mixed models	$k$ - $\varepsilon$ -model $k$ - $\Omega$ -model hybrides (SST) (isotropic)	Reynolds Analogy	current	isotropic in all scales WF, mesh,
		$Pr_t$ -correlations $Pr_t=f(Re, Pr, y^+)$ +adequate wall functions for $T^+$	near	
TMBF model	$k$ - $\varepsilon$ -model (isotropic)	Transport equations $\overline{u'T'}, \overline{T'^2}, \varepsilon_{T'}$ (still problems with temp. variance dissipation)	near not in comm. codes	performance in conv. purely buoy. flow ? + low $Pe$ ?
mixed higher order	kubic $k$ - $\varepsilon$ -model	Transport equations $\overline{u'T'}, \overline{T'^2}, \varepsilon_{T'}$ (Constants fort ransport eq. from DNS)	req. scientific benchmark	promising results (lacking exp. data)
	ASM			
	RSM			
Exact solution	DNS	DNS	future benchmark	



0<sup>th</sup> order direct coupling



2<sup>nd</sup> order Tensorial GDH



1<sup>st</sup> order Gradient diffusion hypothesis

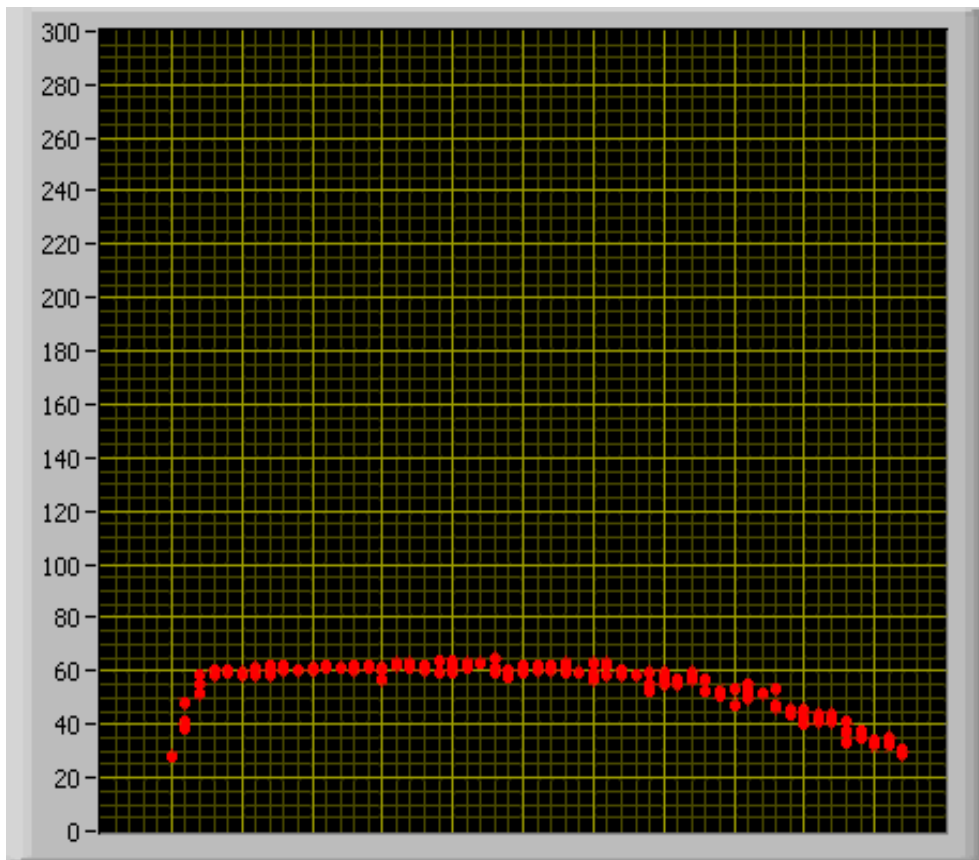


exact solutions

- Model coefficients depend also (!) on  $Re$ ,  $Pr$ , geometry
- Similar classification for LES

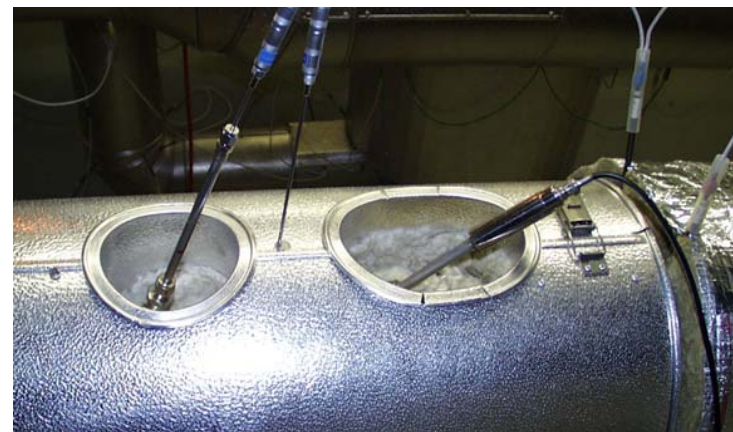


## Velocity : Ultra-Sound Doppler Velocimeter (UDV)



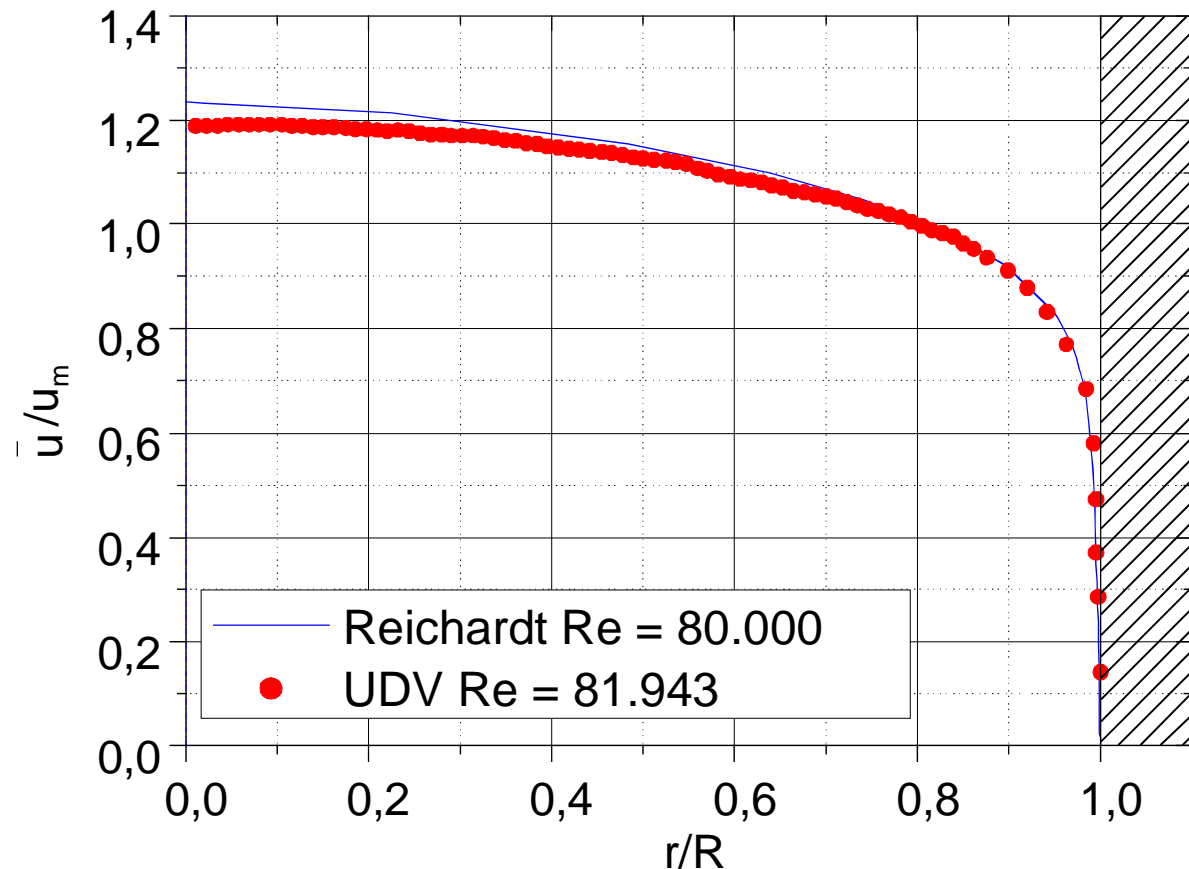
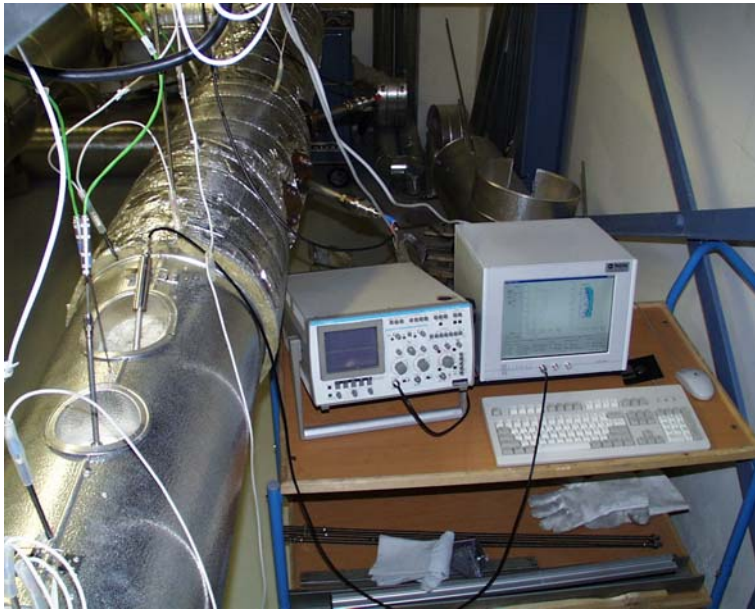
Transient start-up behaviour of  
EM pump in THESYS Loop

- Fluid temperature: 400°C
- Temperatur compensation durch (Wave Guide)
- Inclination angle: 45°
- Tube diameter: 60 mm





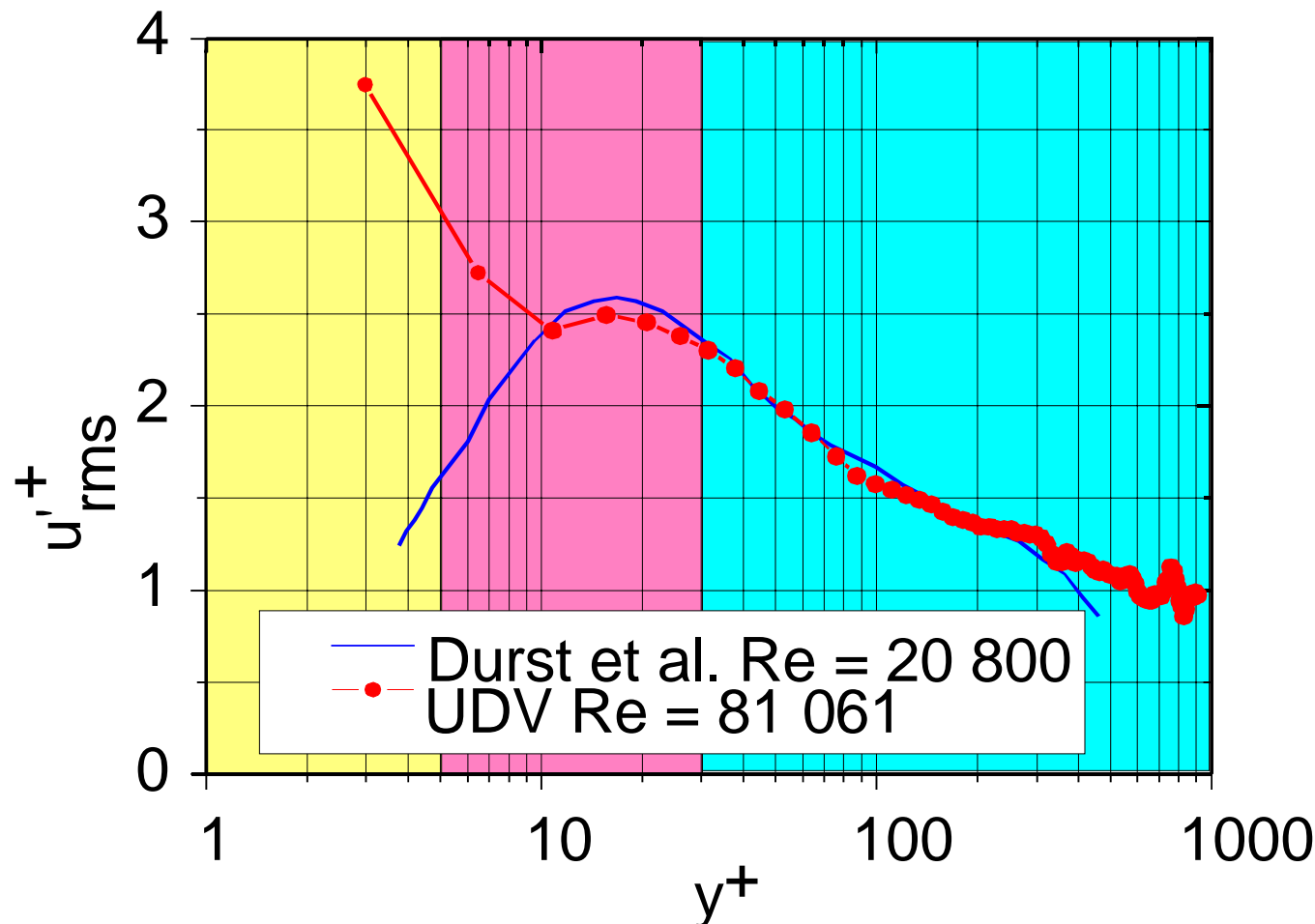
## Velocity: Ultra-Sound Doppler Velocimeter (UDV)



- Excellent agreement between measurement and literature profile
- Detailed resolution of the velocity profile
- Deviation from literature profile for  $r/R > 0.6$  less than 0.5%



# UDV Fluctuation measurements in boundary layer in a tube





# Supporting Water experiments

# HYTAS

$Re_{\text{inflow,gap}} = 60.000$

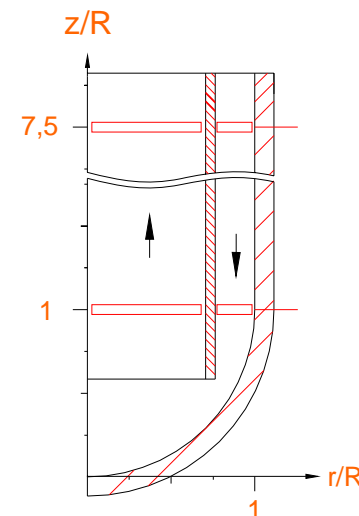
$Q_{\text{main}} / Q_{\text{bypass}} = 15 / 1$

## Simulation of the momentum exchange in MEGAPIE

- Optimization of the nozzle (Geometry, Location).
- Determination of best operation point ratio of main to jet flow rate.
- Verification of CFD simulation for momentum transport



Experiments in transparent media at the same Reynolds- numbers using optic methods (LDA,LLS,UDV)







# Axial Velocity Profile down the riser pipe at $\phi=0^\circ$

## Experimental Set-UP

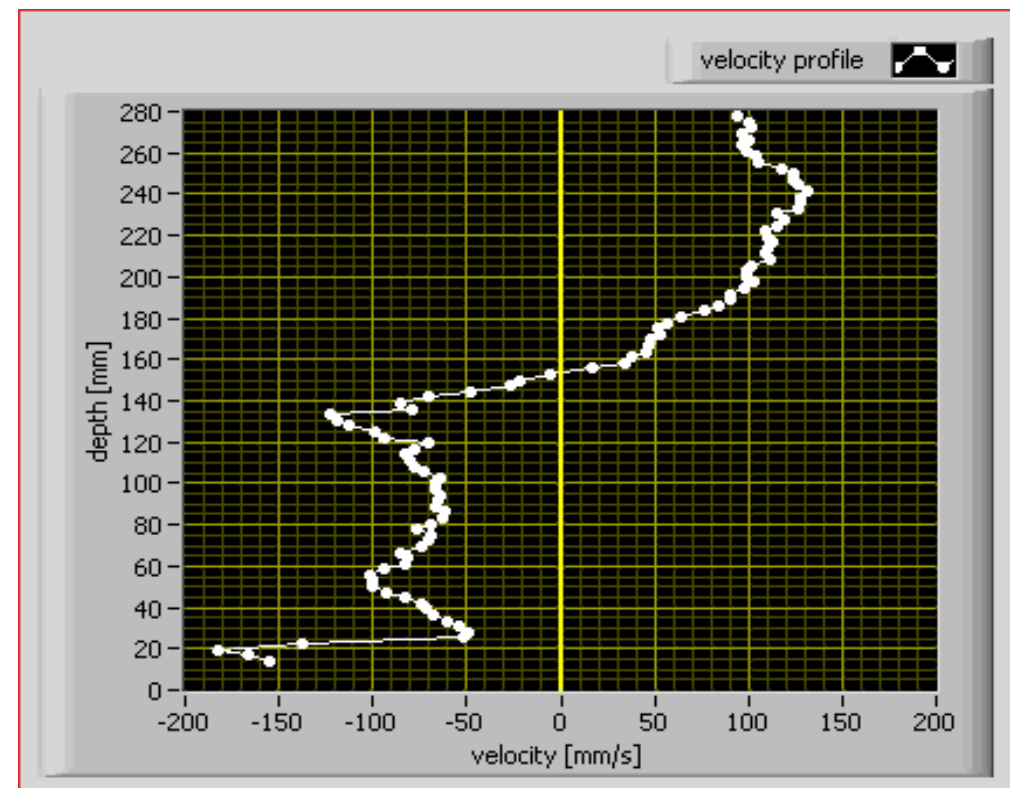
- UDV technique
- 4MHz sensor parallel to the riser pipe at  $\phi=0^\circ$  ( $r/R=0.66$ )
- $Re=5.2 \cdot 10^4$

## Observation

- Highly turbulent flow
- Oscillation of the stagnation point along the riser tube.
- Time dependent two stagnation points appear.

## RESULT

- Strong time dependence (LES started)





# OUTLOOK- LIQUID METAL FLOWS

- So far only single phase heat transfer considered.
- But, advanced technical concepts in nuclear community and industrial processes involve new physical aspects, which are of challenging character, such as
  - Free surface flows
  - Two-phase flows
  - Freezing/remelting

